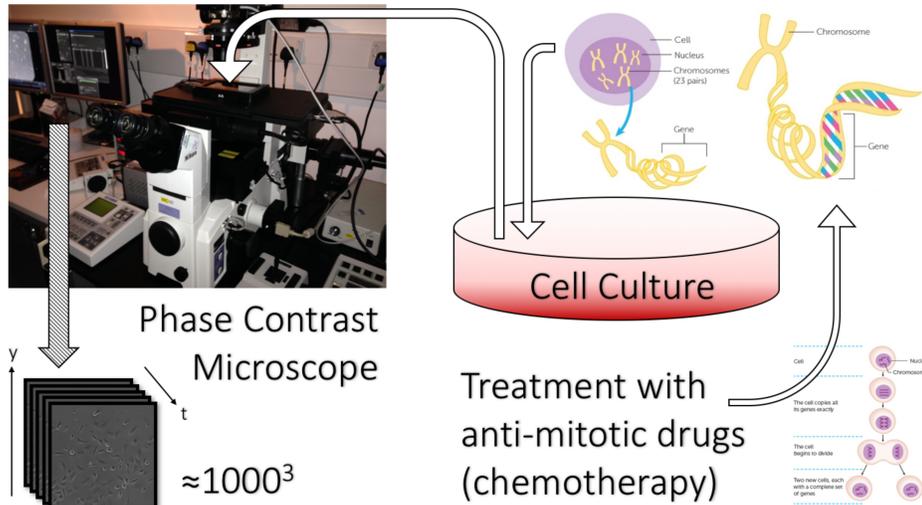


Mathematical Imaging Methods for Mitosis Analysis in Live-Cell Phase Contrast Microscopy

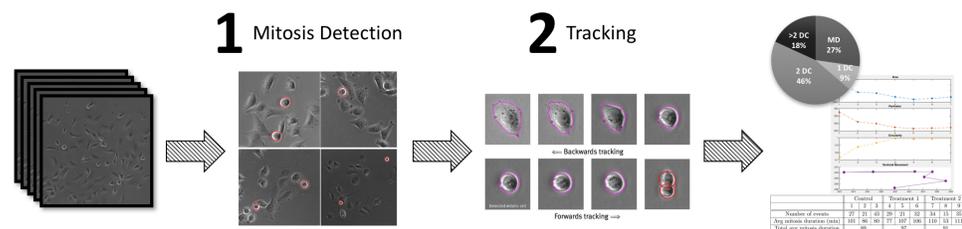
Joana Grah¹, Jennifer Harrington², Siang Boon Koh², Jeremy Pike², Alexander Schreiner², Martin Burger³, Carola-Bibiane Schönlieb¹, Stefanie Reichelt²
¹ Department of Applied Mathematics and Theoretical Physics, University of Cambridge. ² Cancer Research UK Cambridge Institute. ³ Institute for Analysis and Numerics, University of Münster, Germany

Motivation



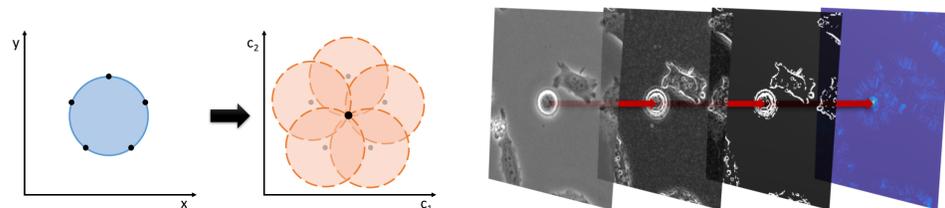
Aim: Determination of average mitosis durations and cell fate distributions

MitosisAnalyser



1 Mitosis Detection

- We are using the **circular Hough transform**, which is an object recognition method for circles in images, in order to detect circularly-shaped mitotic cells
- During this procedure, cell locations are determined from **maxima** of the circular Hough transform applied to an **edge map** of the underlying image



2 Tracking

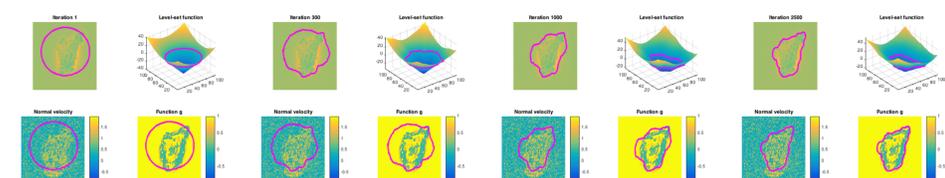
- The circular contour obtained in Step 1 is used as an **initialisation** for the segmentation in Step 2, where cells are first tracked **backwards** in time until the beginning and subsequently **forwards** in time until the end of mitosis
- Using **variational and level-set methods**, we aim at minimising the following energy functional incorporating information on the tracking contour evolution, which shall lead to coincidence of the contour with the cell membrane:

$$\lambda_1 \int_{\Omega} (c_1 - |v|)^2 (1 - H(\phi(x))) dx + \lambda_2 \int_{\Omega} (c_2 - |v|)^2 H(\phi(x)) dx + \mu \int_{\Omega} |\nabla H(\phi(x))| dx$$

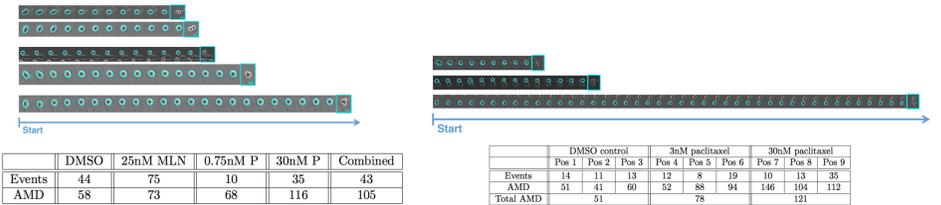
partition into two regions with different normal velocities
small contour length

$$+ \nu \int_{\Omega} g(f(x)) |\nabla H(\phi(x))| dx + \omega \frac{1}{2} \max \left\{ \int_{\Omega} (1 - H(\phi(x))) dx - t_{\text{area}}, 0 \right\}^2 \rightarrow \min_{\phi, c_1, c_2}$$

stop contour at edges based on loc std
keep area above threshold

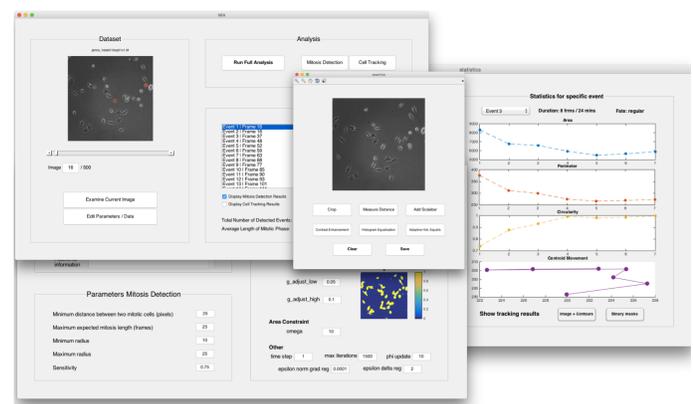
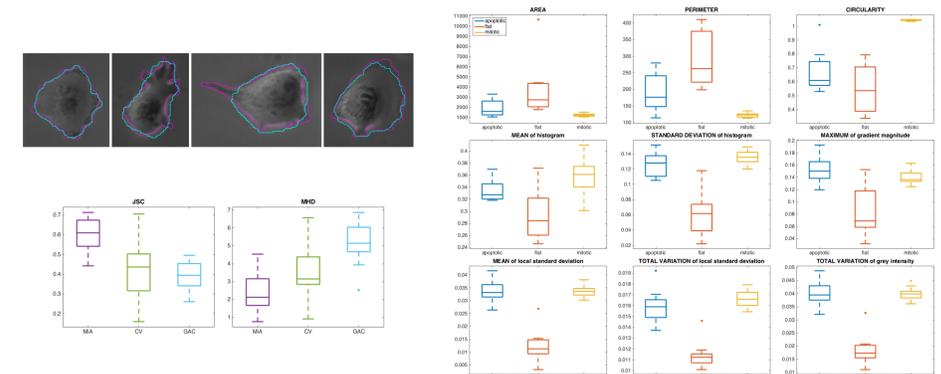


Results



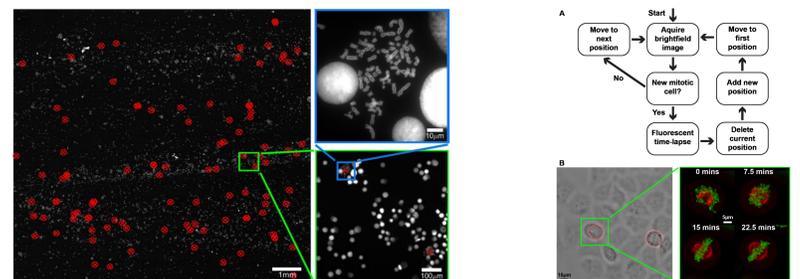
Left: Phase contrast microscopy experiment with HeLa Aur A cells

Right: Multi-modality experiment with Fucci-expressing MIA PaCa-2 cells



JG, J. Harrington, S. B. Koh, J. Pike, A. Schreiner, M. Burger, C.-B. Schönlieb, S. Reichelt. Mathematical Imaging Methods for Mitosis Analysis in Live-Cell Phase Contrast Microscopy. *Methods*, 115: 91-99, 2017.

Outlook: Multi-Modal On-Line Processing



J. Pike, P. Mascalchi, JG, S. Reichelt. Event Driven Automated Microscopy. Applications in Cancer Research. *Imaging & Microscopy*, 2017.

References

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[2] P. V. C. Hough. Method and means for recognizing complex patterns, December 18 1962. US Patent 3,069,654.

[3] M. Möller, M. Burger, P. Dieterich and A. Schwab. A framework for automated cell tracking in phase contrast microscopic videos based on normal velocities. *Journal of Visual Communication and Image Representation*, 25(2):396-409, 2014.